

MATH 16A MIDTERM 1(PRACTICE 2)
PROFESSOR PAULIN

**DO NOT TURN OVER UNTIL
INSTRUCTED TO DO SO.**

CALCULATORS ARE NOT PERMITTED

**YOU MAY USE YOUR OWN BLANK
PAPER FOR ROUGH WORK**

**SO AS NOT TO DISTURB OTHER
STUDENTS, EVERYONE MUST STAY
UNTIL THE EXAM IS COMPLETE**

**REMEMBER THIS EXAM IS GRADED BY
A HUMAN BEING. WRITE YOUR
SOLUTIONS NEATLY AND
COHERENTLY, OR THEY RISK NOT
RECEIVING FULL CREDIT**

**THIS EXAM WILL BE ELECTRONICALLY
SCANNED. MAKE SURE YOU WRITE ALL
SOLUTIONS IN THE SPACES PROVIDED.
YOU MAY WRITE SOLUTIONS ON THE
BLANK PAGE AT THE BACK BUT BE
SURE TO CLEARLY LABEL THEM**

Name and section: _____

GSI's name: _____

This exam consists of 5 questions. Answer the questions in the spaces provided.

1. (25 points) (a) Determine the equation of the straight (in the xy -plane) which contains the points $(1, 4)$ and $(-1, 3)$

Solution:

- (b) Calculate the x -intercept of the straight line containing $(3, 2)$, which is perpendicular to the line in (a).

Solution:

2. (25 points) A product is to be produced and sold. The cost function $C(x)$ is linear, with marginal cost of 1 and fixed cost of 4. The revenue function is

$$R(x) = x^2 + x$$

- (a) Determine the break-even quantity.

Solution:

- (b) What is the marginal profit at this quantity? You must calculate this from first principles using limits.

Solution:

PLEASE TURN OVER

3. Calculate the following limits. If they do not exist determine if they are ∞ or $-\infty$.

(a)

$$\lim_{x \rightarrow -1} \frac{x^2 + 3x + 2}{x^2 - x - 2}$$

Solution:

(b)

$$\lim_{x \rightarrow -\infty} \sqrt[3]{\frac{4x}{7x^2 + 5}}$$

Solution:

(c)

$$\lim_{x \rightarrow 1^-} \frac{1 - x}{x^2 - 2x + 1}$$

Solution:

PLEASE TURN OVER

4. Let $f(x) = \begin{cases} \frac{x-1}{\sqrt{x-1}} + a^2 & \text{if } x > 1 \\ a - x^2 & \text{if } x \leq 1 \end{cases}$ for some real number a .

Is it possible to choose a real number a such that $f(x)$ continuous at $x = 1$? Carefully justify your answer.

Solution:

5. Using limits, calculate the derivative of $f(x) = \frac{x}{x+1}$. Determine the points on the graph $y = f(x)$ where the slope of the tangent line is 2.

Solution: